Suppose  $f(x, y) = x^2 + y^2 - 8x - 8y + 1$ .

- (A) How many critical points does f have in  $\mathbb{R}^2$ ?
- (B) If there is a local minimum, what is the value of the discriminant D at that point? If there is none, type N.
- (C) If there is a local maximum, what is the value of the discriminant D at that point? If there is none, type N.
- (D) If there is a saddle point, what is the value of the discriminant D at that point? If there is none, type N.
- (E) What is the maximum value of f on  $\mathbb{R}^2$ ? If there is none, type N.
- (F) What is the minimum value of f on  $\mathbb{R}^2$ ? If there is none, type N.

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(F) What is the minimum value of f on  $\mathbb{R}^2$ ? If there is none, type N.

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